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## Addition and Subtraction of Fractions and Mixed Numbers

#### Adding and Subtracting Fractions:

- 1) Rewrite the fractions with a common denominator
- 2) Add or subtract the numerators
- 3) Simplify the fraction

$$\frac{\cancel{3} + \cancel{6}}{\cancel{3} \cancel{2}} \frac{\cancel{2}}{\cancel{6}}$$

$$\frac{\frac{1}{6} \times 1}{\frac{1}{6}} \frac{1}{6}$$

$$\frac{3}{6} \div \frac{3}{3} \frac{1}{2}$$

#### Adding and Subtracting Mixed Numbers:

- Rewrite the fractions with a common denominator
- 2) Rename, if necessary
- 3) Add or subtract the fractions. Add or subtract the whole numbers
- 4) Simplify if necessary

$$3\frac{1}{4} - 1\frac{1}{3}$$

$$3\frac{1}{4} = \cancel{3}\frac{3}{12} + \frac{12}{12} = 2\frac{15}{12}$$
$$-1\frac{1}{3} = 1\frac{4}{12} = 1\frac{4}{12}$$

 $1\frac{11}{12}$ 

Find the sum. Write your answer in simplest form.

1. 
$$\frac{1}{4} + \frac{1}{2}$$

2. 
$$\frac{2}{5} + \frac{1}{3}$$

1. 
$$\frac{1}{4} + \frac{1}{2}$$
 2.  $\frac{2}{5} + \frac{1}{3}$  3.  $\frac{7}{15} + \frac{3}{10}$  4.  $\frac{11}{28} + \frac{4}{7}$ 

$$4. \frac{11}{28} + \frac{4}{7}$$

5. 
$$\frac{3}{4} + \frac{1}{12}$$

6. 
$$\frac{9}{10} + \frac{13}{20}$$

7. 
$$4\frac{15}{16} + 7\frac{3}{4}$$

5. 
$$\frac{3}{4} + \frac{1}{12}$$
 6.  $\frac{9}{10} + \frac{13}{20}$  7.  $4\frac{15}{16} + 7\frac{3}{4}$  8.  $2\frac{16}{25} + 3\frac{18}{20}$ 

9. 
$$3\frac{2}{5} + 9\frac{1}{10}$$

9. 
$$3\frac{2}{5} + 9\frac{1}{10}$$
 10.  $6\frac{1}{42} + 4\frac{5}{6}$  11.  $18\frac{7}{9} + 16$  12.  $4\frac{7}{8} + \frac{1}{3}$ 

11. 
$$18\frac{7}{9} + 16$$

12. 
$$4\frac{7}{8} + \frac{1}{3}$$

Find the difference. Write your answer in simplest form

13. 
$$\frac{7}{8} - \frac{1}{4}$$

14. 
$$\frac{13}{15} - \frac{1}{3}$$

15. 
$$\frac{7}{9} - \frac{2}{6}$$

13. 
$$\frac{7}{8} - \frac{1}{4}$$
 14.  $\frac{13}{15} - \frac{1}{3}$  15.  $\frac{7}{9} - \frac{2}{6}$  16.  $\frac{21}{24} - \frac{3}{8}$ 

17. 
$$\frac{3}{14} - \frac{1}{7}$$

18. 
$$\frac{9}{10} - \frac{1}{2}$$

19. 
$$9\frac{1}{6} - 4\frac{1}{12}$$

17. 
$$\frac{3}{14} - \frac{1}{7}$$
 18.  $\frac{9}{10} - \frac{1}{2}$  19.  $9\frac{1}{6} - 4\frac{1}{12}$  20.  $12\frac{18}{25} - 8\frac{4}{5}$ 

21. 
$$5\frac{8}{9} - 3\frac{2}{3}$$

21. 
$$5\frac{8}{9} - 3\frac{2}{3}$$
 22.  $8\frac{12}{16} - 7\frac{31}{32}$  23.  $10\frac{3}{4} - 6\frac{4}{5}$  24.  $13\frac{7}{8} - \frac{10}{12}$ 

23. 
$$10\frac{3}{4} - 6\frac{4}{5}$$

24. 
$$13\frac{7}{8} - \frac{10}{12}$$

# Multiplication and Division of Fractions and Mixed Numbers

#### Multiplying Fractions and Mixed Numbers:

- 1) Convert mixed numbers to improper fractions
- 2) Cross simplify if possible
- 3) Multiply the 2 numerators and then multiply the 2 denominators
- 4) Simplify if necessary

$$2\frac{1}{4} \cdot \frac{1}{3}$$

$$2\frac{1}{4} = \frac{9}{4}$$

$$\begin{array}{c} 3 & \cancel{9} \\ 4 & \cancel{3} \end{array} = \begin{array}{c} 3 \\ 4 \end{array}$$

#### Dividing Fractions and Mixed Numbers:

- 1) Convert mixed numbers to improper fractions
- 2) "Same, Change, Flip" (keep first fraction the same, change division to multiplication, flip second fraction to its reciprocal)
- 3) Cross simplify if possible and then multiply
- 4) Simplify if necessary

$$\frac{3}{7} \div \frac{9}{10}$$

$$\frac{1}{7} \cdot \frac{10}{9_3} = \frac{10}{21}$$

Find the product. Write your answer in simplest form

25. 
$$\frac{1}{8} \cdot \frac{1}{7}$$

26. 
$$\frac{2}{9} \cdot \frac{12}{14}$$

$$27. \quad \frac{7}{12} \cdot \frac{8}{14}$$

26. 
$$\frac{2}{9} \cdot \frac{12}{14}$$
 27.  $\frac{7}{12} \cdot \frac{8}{14}$  28.  $\frac{9}{24} \cdot \frac{16}{81}$ 

29. 
$$\frac{3}{14} \cdot \frac{21}{33}$$

30. 
$$\frac{1}{2} \cdot \frac{9}{13}$$

31. 
$$2\frac{1}{6} \cdot \frac{3}{5}$$

29. 
$$\frac{3}{14} \cdot \frac{21}{33}$$
 30.  $\frac{1}{2} \cdot \frac{9}{13}$  31.  $2\frac{1}{6} \cdot \frac{3}{5}$  32.  $8\frac{4}{5} \cdot 1\frac{5}{11}$ 

$$33. \quad 2\frac{1}{2} \cdot \frac{2}{5}$$

34. 
$$9\frac{2}{3} \cdot 6$$

33. 
$$2\frac{1}{2} \cdot \frac{2}{5}$$
 34.  $9\frac{2}{3} \cdot 6$  35.  $13\frac{1}{3} \cdot 2\frac{1}{10}$  36.  $7 \cdot \frac{1}{3}$ 

36. 
$$7 \cdot \frac{1}{3}$$

Find the quotient. Write your answer in simplest form

37. 
$$\frac{5}{6} \div \frac{1}{4}$$

$$38. \quad \frac{1}{2} \div \frac{1}{4}$$

39. 
$$\frac{3}{4} \div \frac{9}{12}$$

37. 
$$\frac{5}{6} \div \frac{1}{4}$$
 38.  $\frac{1}{2} \div \frac{1}{4}$  39.  $\frac{3}{4} \div \frac{9}{12}$  40.  $\frac{21}{35} \div \frac{7}{25}$ 

41. 
$$\frac{6}{7} \div 3$$

42. 
$$\frac{2}{11} \div \frac{1}{33}$$

41. 
$$\frac{6}{7} \div 3$$
 42.  $\frac{2}{11} \div \frac{1}{33}$  43.  $1\frac{1}{4} \div 2\frac{1}{3}$  44.  $5\frac{3}{6} \div 3$ 

44. 
$$5\frac{3}{6} \div 3$$

45. 
$$10\frac{1}{4} \div \frac{2}{5}$$

45. 
$$10\frac{1}{4} \div \frac{2}{5}$$
 46.  $3\frac{2}{3} \div 1\frac{1}{7}$  47.  $4\frac{3}{8} \div \frac{9}{10}$  48.  $8 \div \frac{3}{4}$ 

47. 
$$4\frac{3}{8} \div \frac{9}{10}$$

48. 
$$8 \div \frac{3}{4}$$

## Operations with Decimals

#### Adding and Subtracting Decimals:

5.2 + 10.03

- 1) Line up decimal points
- 2) Bring the decimal down
- 3) Add or subtract as if numbers are whole numbers

#### Multiplying Decimals:

- 1) Ignore the decimal points
- 2) Multiply as if numbers are whole numbers
- 3) Count the number of decimal places in the problem and move the decimal point in answer that many places

$$1.03 \times 2.8$$

$$\begin{array}{r}
1.03 \\
 \hline
2.8 \\
\hline
824
\end{array}$$

2060 2884

#### Dividing Decimals:

- 1) If there is a decimal in the divisor, move it to the end of the number and move the decimal in the dividend the same number of places
- 2) Bring decimal point in dividend straight up.
- 3) Divide Add zeros to dividend and bring down if necessary.

$$6.4 \div 1.2$$

$$\begin{array}{c|c}
5 & \overline{3} \\
\hline
1.2)6.4.0 \\
\underline{60} & \downarrow \\
4 & 0 \\
\underline{36} \\
4
\end{array}$$

#### Find the sum or difference.

49. 
$$6.2 + 3.4$$

50. 
$$8.04 - 6.8$$

$$51. 12.4 + 0.899$$

$$8.04 - 6.8$$
 51.  $12.4 + 0.899$  52.  $12.9 - 2.043$ 

$$54. 13-6.7$$

55. 
$$3.91+1.93$$

$$3.91 + 1.93$$
 56.  $34.2 - 29.027$ 

#### Find the product.

57. 
$$9.2 \times 3.1$$

$$(14.1)(2.7)$$
 59.  $91 \times 4.5$  60.  $(82.04)(1.2)$ 

62. 
$$45 \times 0.1$$

$$45 \times 0.1$$
 63.  $0.010 \times 13.9$ 

#### Find the quotient.

65. 
$$2)8.4$$

$$2)8.4$$
 66.  $13)1.56$  67.  $2)7.45$  68.  $8)9$ 

68. 
$$8)9$$

69. 
$$3.4)68$$

$$3.4)68$$
 70.  $0.2)9.4$ 

$$0.2\overline{)9.4}$$
 71.  $0.15\overline{)0.045}$ 

72. 
$$0.3)4$$

## Geometry

#### Area Formulas: (remember area = the space inside a figure)

 $Area of Rectangle = length \times width$ 

Area of Triangle =  $\frac{1}{2}base \times height$ 

Area of Circle =  $\pi \cdot radius^2$ 

 $Area\ of\ Parallelogram = base \times height$ 

#### Perimeter: (remember perimeter = the distance around a figure)

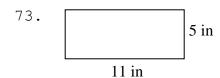
Perimeter of any polygon: add up all the sides

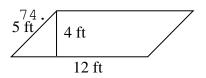
Circumference of Circle =  $2 \cdot \pi \cdot radius$ 

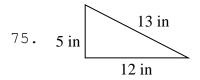
#### Volume: (remember volume = the capacity of a 3D figure)

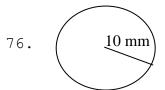
Volume of Rectangular Prism =  $length \times width \times height$  $\pi \cdot diameter$ 

#### Find the area and perimeter (or circumference). Use 3.14 for pi:









#### Find the volume:

#### Solve the word problem:

- 78. Danny is installing a fence around his rectangular yard. His yard is 20 feet long by 45 feet wide. If the fencing he picked out costs \$25 per foot, how much money will Danny spend on the fence?
- 79. Tameka wants to put a carpet in her rectangular bedroom. Her room is 22 feet long by 18 feet wide. How much carpeting will Tameka need?
- 80. Don wants to bring some sand home from his vacation at the beach. He has a box that is 3 inches wide, 4 inches long, and 2 inches tall. How much sand can he fit in the box?

## Solving One-step Equations

#### Addition Equations:

Subtract the number on the same side of the equal sign as the variable from each side of the equation

$$x + 3 = 9$$

$$\begin{array}{c}
x + 3 = 9 \\
-3 - 3
\end{array}$$

#### Subtraction Equations:

Add the number on the same side of the equal sign as the variable to each side of the equation

$$14 = x - 7$$

#### Multiplication Equations:

Divide each side of the equation by the number on the same side of the equal sign as the variable

$$\boxed{5m = 105}$$

$$\frac{5}{5}m = \underline{105}$$

$$\boxed{m = 21}$$

#### Division Equations:

Multiply each side of the equation by the number on the same side of the equal sign as the variable

$$\boxed{\frac{y}{13} = 5}$$

$$13 \times \frac{y}{13} = 5 \times 13$$

$$y = 65$$

#### Solve for the given variable:

81. 
$$x+18=32$$

82. 
$$18f = 720$$

33. 
$$h-56=57$$

81. 
$$x+18=32$$
 82.  $18f=720$  83.  $h-56=57$  84.  $\frac{b}{6}=12$ 

85. 
$$12 = r - 76$$

85. 
$$12 = r - 76$$
 86.  $33 + d = 65$  87.  $14m = 42$  88.

87. 
$$14m = 42$$

88. 
$$10c = 5$$

89. 
$$38 = 19i$$

89. 
$$38 = 19j$$
 90.  $w + 65 = 100$  91.  $r - 7 = 9$  92.  $x \div 12 = 9$ 

91. 
$$r-7=9$$

92. 
$$x \div 12 = 9$$

93. 
$$14 + x = 18$$

93. 
$$14 + x = 18$$
 94.  $\frac{p}{22} = 7$  95.  $47 = x - 5$  96.  $k + 16 = 76$ 

95. 
$$47 = x - 5$$

96. 
$$k+16=76$$

97. 
$$2 = 6m$$

98. 
$$t-8=14$$

99. 
$$\frac{h}{19} = 11$$

97. 
$$2 = 6m$$
 98.  $t - 8 = 14$  99.  $\frac{h}{19} = 11$  100.  $47 = 18 + b$ 

### Answer Key

1	3
1.	- 4

5. 
$$\frac{5}{6}$$

9. 
$$12\frac{1}{2}$$

13. 
$$\frac{5}{8}$$

17. 
$$\frac{1}{14}$$

**21.** 
$$2\frac{2}{9}$$

25. 
$$\frac{1}{56}$$

29. 
$$\frac{3}{22}$$

37. 
$$3\frac{1}{3}$$

**41**. 
$$\frac{2}{7}$$

**45**. 
$$25\frac{5}{8}$$

97. 
$$m=^{1}/_{3}$$

2. 
$$\frac{11}{15}$$

6. 
$$1\frac{11}{20}$$

10. 
$$10\frac{6}{7}$$

14. 
$$\frac{8}{15}$$

18. 
$$\frac{2}{5}$$

22. 
$$\frac{25}{32}$$

26. 
$$\frac{4}{21}$$

30. 
$$\frac{9}{26}$$

**46**. 
$$3\frac{5}{24}$$

3. 
$$\frac{23}{30}$$

7. 
$$12\frac{11}{16}$$

11. 
$$34\frac{7}{9}$$

15. 
$$\frac{4}{9}$$

19. 
$$5\frac{1}{12}$$

**23**. 
$$3\frac{19}{20}$$

27. 
$$\frac{1}{3}$$

**31.** 
$$1\frac{3}{10}$$

43. 
$$\frac{15}{28}$$

**47.** 
$$4\frac{31}{36}$$

4. 
$$\frac{27}{28}$$

8. 
$$6\frac{27}{50}$$

12. 
$$5\frac{5}{24}$$

16. 
$$\frac{1}{2}$$

**20.** 
$$3\frac{23}{25}$$

**24.** 
$$13\frac{1}{24}$$

28. 
$$\frac{2}{27}$$

32. 
$$12\frac{4}{5}$$

36. 
$$2\frac{1}{3}$$

**40**. 
$$2\frac{1}{7}$$

**44.** 
$$1\frac{5}{6}$$

**48.** 
$$10\frac{2}{3}$$

88. 
$$c=\frac{1}{2}$$